

Einführung in die Erweiterte Realität

- 1. Introduction -
will be held on Oct 28, 2003

- 2. Coordinate Systems -

Gudrun Klinker

Oct 21, 2003

Agenda

1. Administrative Issues
2. Coordinate Systems

1. Administrative Issues

- Lecture:
Tuesdays 9:15 - 10:45
- Schein:
Oral exam
- Office hours:
By appointment
- Infos:
www.bruegge.in.tum.de/projects/lehrstuhl/twiki/bin/view/Lehrstuhl/AugmentedRealityIntroductionWiSe2003

or via:
www.in.tum.de/~klinker -> Teaching -> Erweiterte Realität I

1. Administrative Issues

- Schedule -

- Oct. 21 Coordinate systems
- Oct. 28 Introduction
- Nov. 4 Computer graphics: OpenGL, VRML
- Nov. 11 Computer graphics: VRML
- Nov. 18 Mixed reality, information presentation
- Nov. 25 Displays (HMDs)
- Dec. 2 System architectures for AR: DWARF
- Dec. 9 System architectures for AR: Context Toolkit
- Dec. 16 Demos

- Jan. 13 Trackers
- Jan. 20 Camera calibration
- Jan. 27 Computer vision
- Feb. 3 Intelligent environments
- Feb. 10 Discussion and conclusions

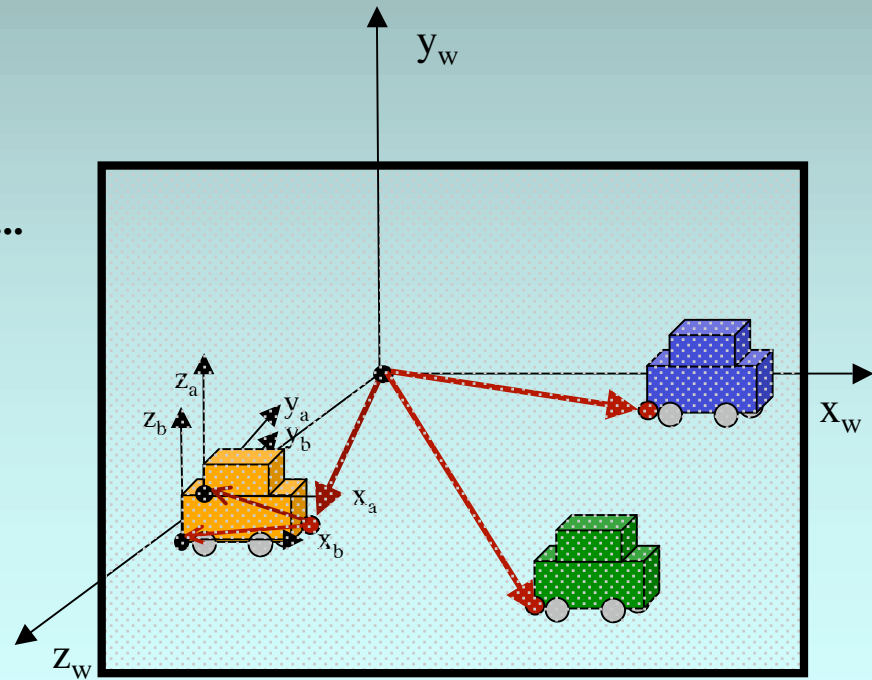
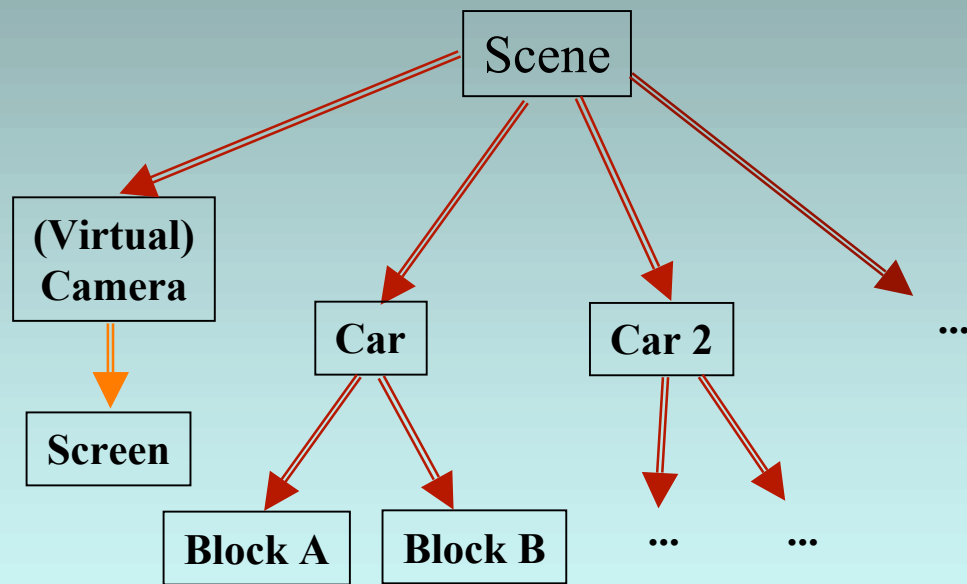
Einführung in die Erweiterte Realität

- 2. Coordinate Systems -

Gudrun Klinker

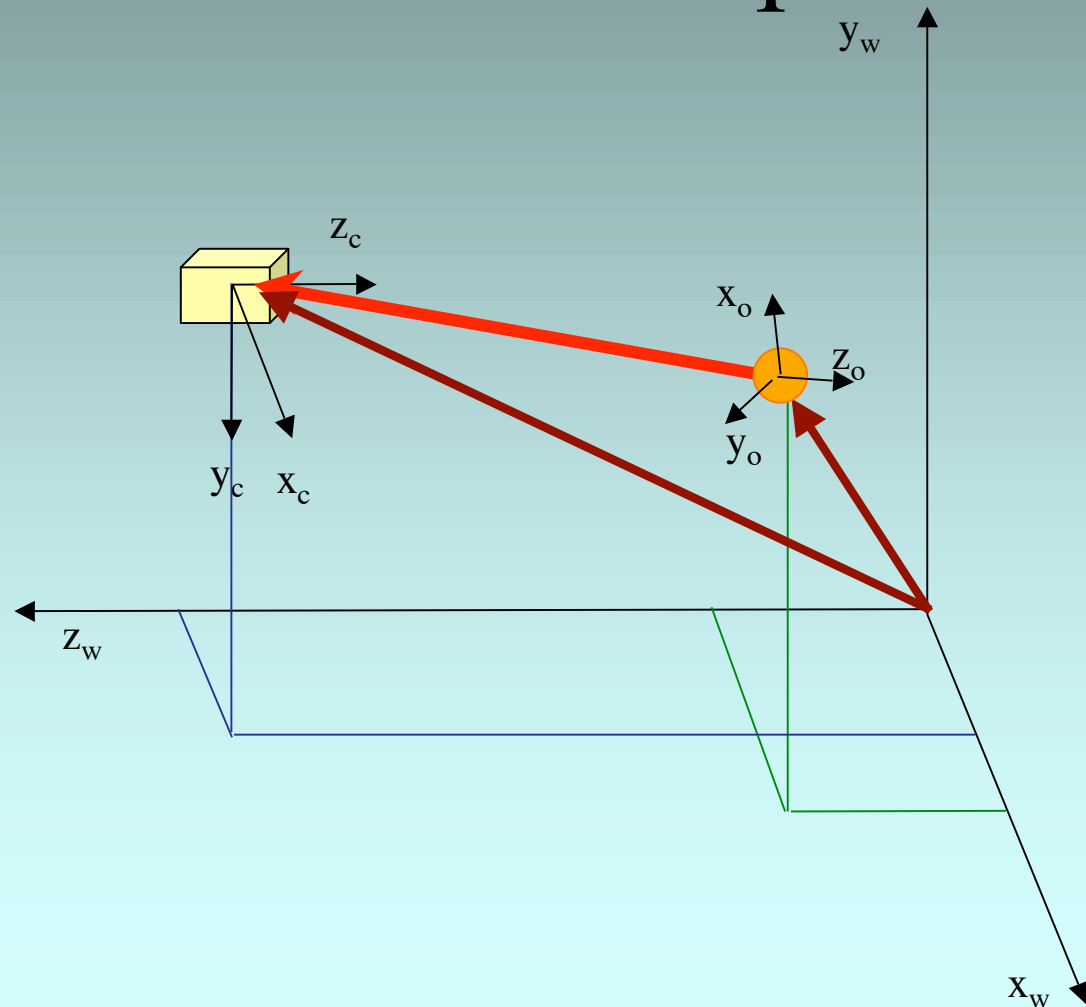
Oct 21, 2003

Scene Graph



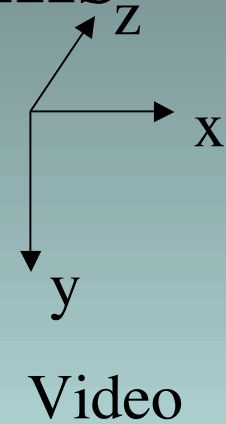
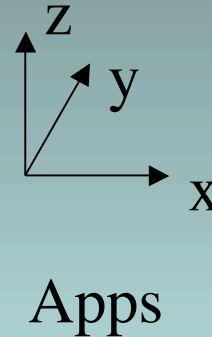
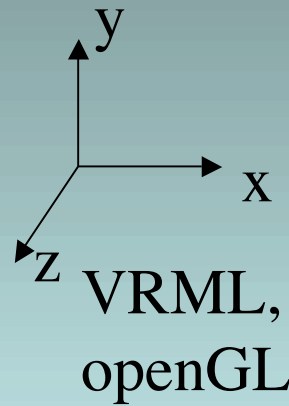
Rendering = Traversal of the Scene Graph

- **Homogeneous coordinates**
3D Transformations between
 - Object coordinates
 - World coordinates
 - Camera coordinates
- **Geometry Pipeline in OpenGL**

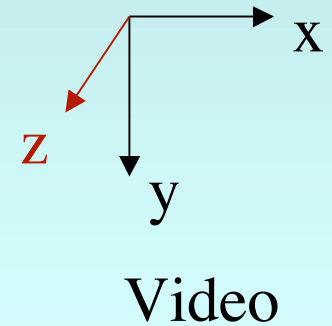
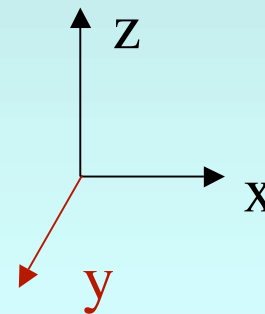
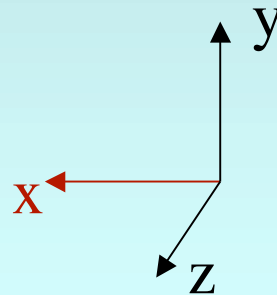


Different Coordinate Systems

- Righthanded Systems

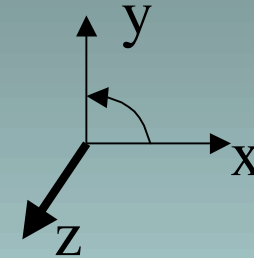


- Lefthanded Systems

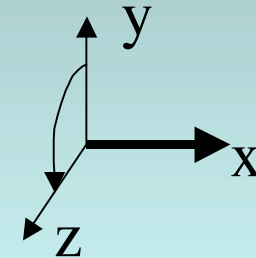


Righthanded Rotations

- Around z: $x \rightarrow y$

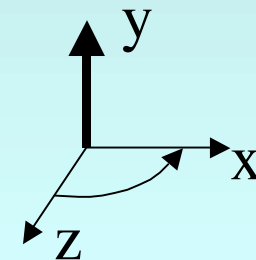


- Around x: $y \rightarrow z$



- Around y: $z \rightarrow x$

X-y-z-x-Y-z-x-y-Z-x-y-z



2D Transformations

- Translation:

$$x_w = x_o + t_x$$

$$y_w = y_o + t_y$$

- Scaling:

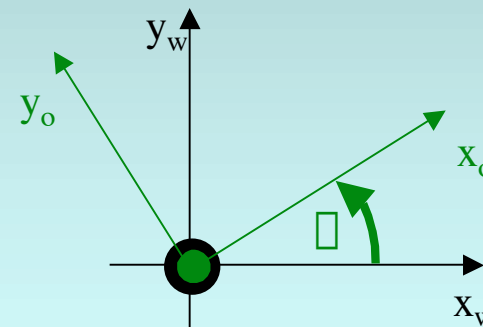
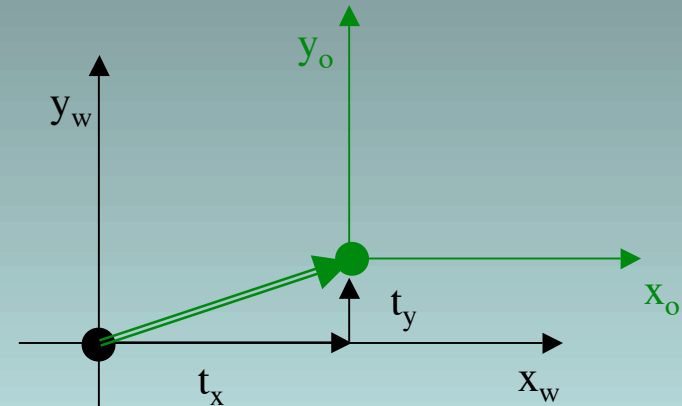
$$x_w = s_x * x_o$$

$$y_w = s_y * y_o$$

- Rotation:

$$x_w = \cos \theta * x_o - \sin \theta * y_o$$

$$y_w = \sin \theta * x_o + \cos \theta * y_o$$



| θ | 0 | 30 | 45 | 60 | 90 |
|----------|-----|--------|--------|--------|-----|
| sin | 0.0 | 0.5 | 0.7071 | 0.8660 | 1.0 |
| cos | 1.0 | 0.8660 | 0.7071 | 0.5 | 0.0 |

2D Transformations Using Homogeneous Coordinates

- Translation:
$$\begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ w \end{bmatrix} = \begin{bmatrix} x + wt_x \\ y + wt_y \\ w \end{bmatrix}$$

- Scaling:
$$\begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ w \end{bmatrix} = \begin{bmatrix} s_x x \\ s_y y \\ w \end{bmatrix}$$

- Rotation:
$$\begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ w \end{bmatrix} = \begin{bmatrix} \cos \theta \cdot x - \sin \theta \cdot y \\ \sin \theta \cdot x + \cos \theta \cdot y \\ w \end{bmatrix}$$

3D Transformations Using Homogeneous Coordinates

- Translation: `glTranslate*` (t_x, t_y, t_z)

$$\begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} x + wt_x \\ y + wt_y \\ z + wt_z \\ w \end{bmatrix}$$

- Scaling: `glScale*` (s_x, s_y, s_z)

$$\begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} s_x x \\ s_y y \\ s_z z \\ w \end{bmatrix}$$

3D Transformations Using Homogeneous Coordinates

- Rotation: $\text{glRotate}^*(\theta, e_x, e_y, e_z)$

– around x

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} x \\ \cos \theta y - \sin \theta z \\ \sin \theta y + \cos \theta z \\ w \end{bmatrix}$$

– around y

$$\begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} \cos \theta x + \sin \theta z \\ y \\ -\sin \theta x + \cos \theta z \\ w \end{bmatrix}$$

– around z

$$\begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} \cos \theta x - \sin \theta y \\ \sin \theta x + \cos \theta y \\ z \\ w \end{bmatrix}$$

Composition of Transformations

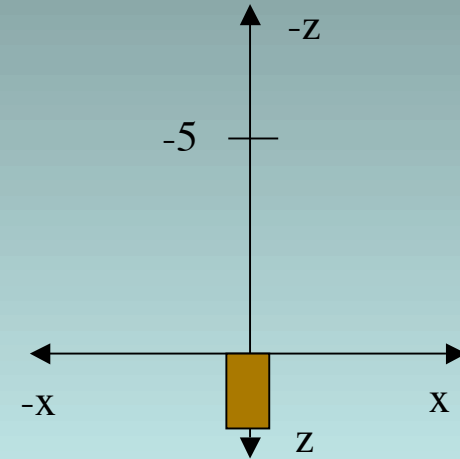
- Initialize accumulative matrix C_0 with identity matrix I
- Post-multiply accumulative matrix C_i with transformation matrix M_i according to command. $C_{i+1} := C_i M_i$
- Accumulated result represents complete transformation (independent of the number of transformation steps)
- Transformation sequence not commutative!!!

Example: translate1 - scale1 - rotate1 - translate2 - rotate2

$$I * T1 * S1 * R1 * T2 * R2 * \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix}$$

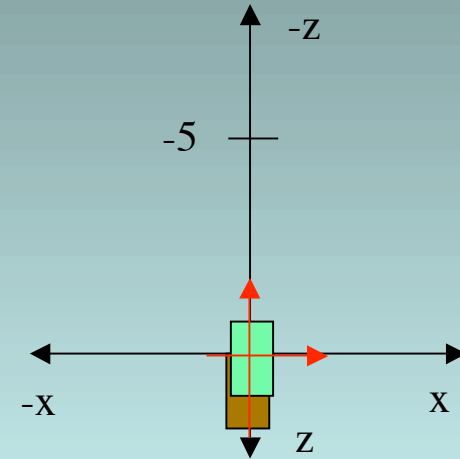
Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```



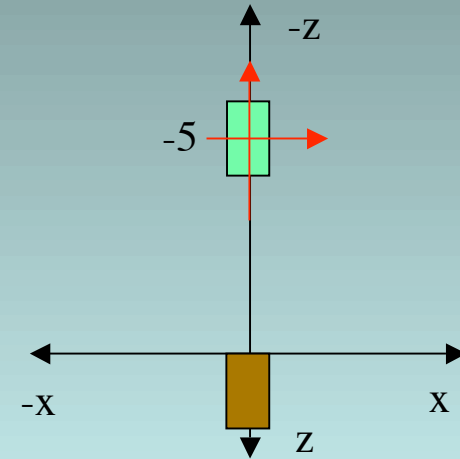
Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```



Viewing/Modelling Transformation Examples

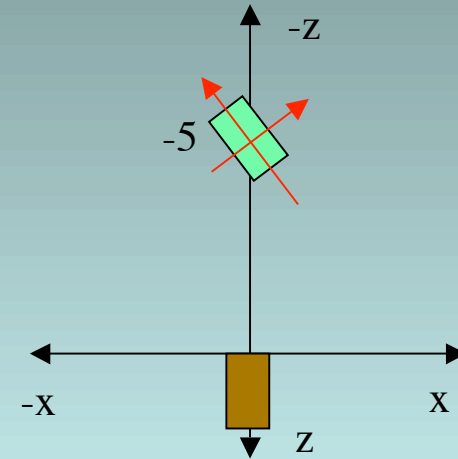
```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```



Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis  
...
```

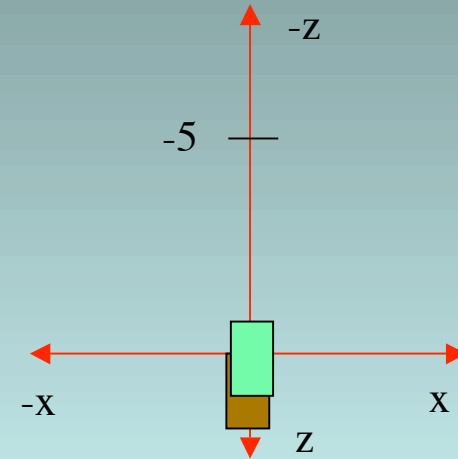
“Examine”



Viewing/Modelling Transformation Examples

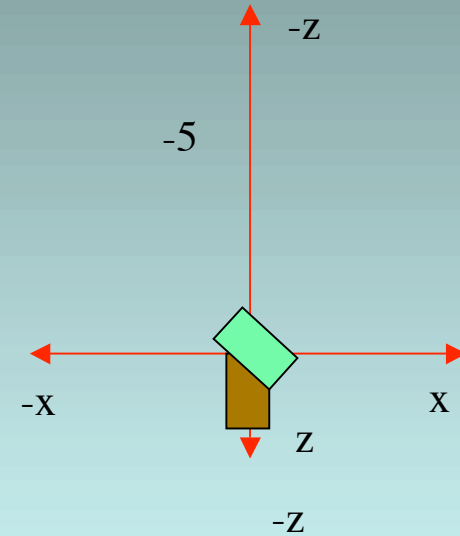
```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```

**ALTERNATIVE:
“Fly-Through”**



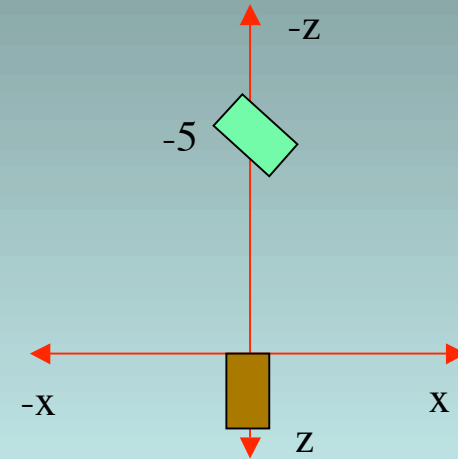
Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```



Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```

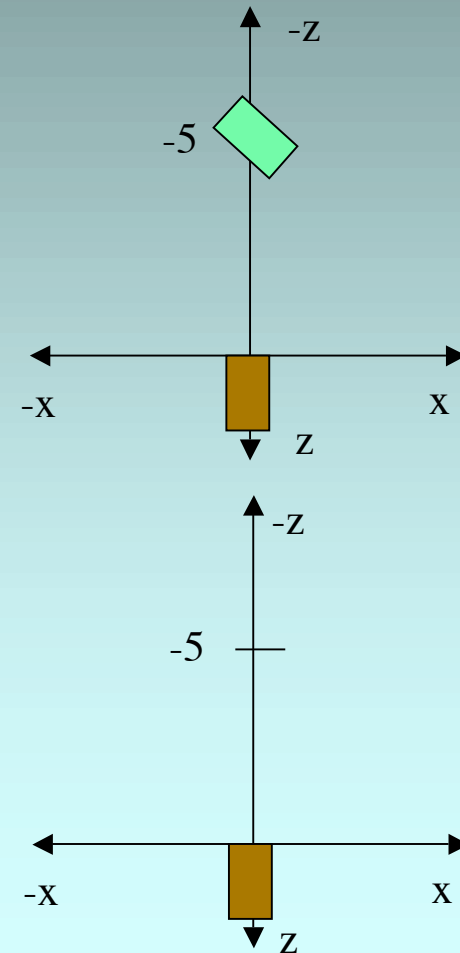


Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```

Question:

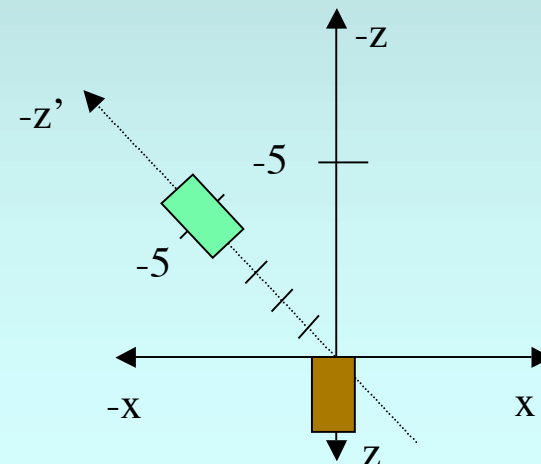
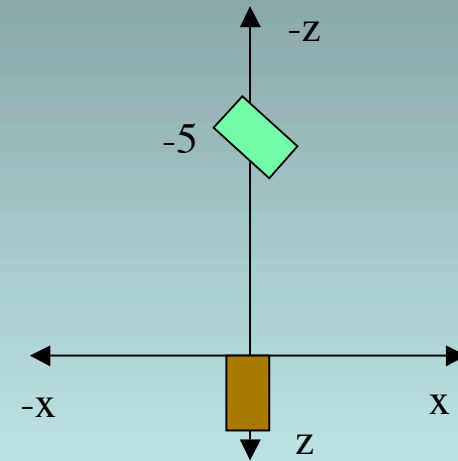
```
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis  
glTranslatef (0.0, 0.0, -5.0); // along z-axis
```



Viewing/Modelling Transformation Examples

```
glTranslatef (0.0, 0.0, -5.0); // along z-axis  
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis
```

```
glRotatef (45.0, 0.0, 1.0, 0.0); // around y-axis  
glTranslatef (0.0, 0.0, -5.0); // along z-axis
```



Transformation Examples

// Flight Simulator, Pilot View (“fly-through”)

// world rotates around stationary camera

...

`glRotated (roll, 0.0, 0.0, 1.0); // z` (4)

`glRotated (pitch, 0.0, 1.0, 0.0); // y` (3)

`glRotated (heading, 1.0, 0.0, 0.0); // x` (2)

`glTranslated (-planex, -planey, -planez);` (1)

// Polar View: rotating camera (= examine object)

// camera rotates around stationary object

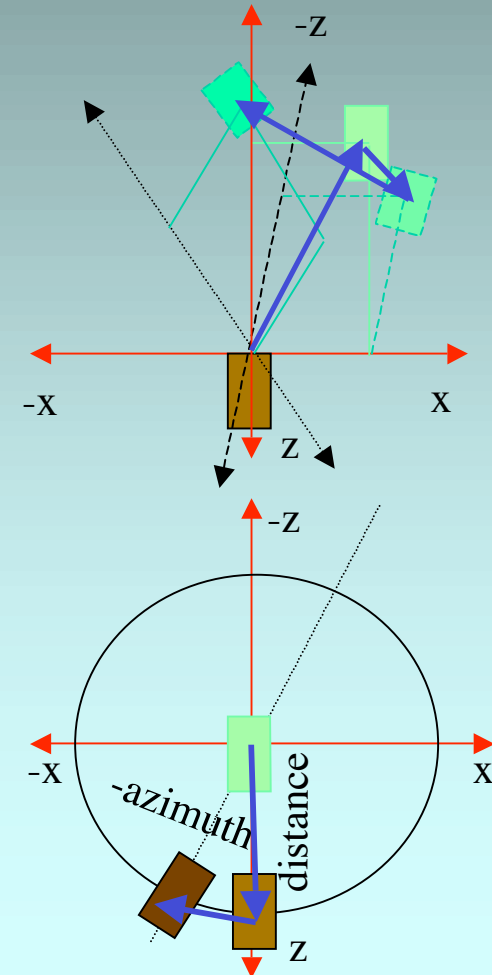
`glTranslated (0.0, 0.0, -distance);` (1)

`glRotated (-twist, 0.0, 0.0, 1.0); // z` (2)

`glRotated (-elevation, 1.0, 0.0, 0.0); // x` (3)

`glRotated (-azimuth, 0.0, 1.0, 0.0); // y` (4)

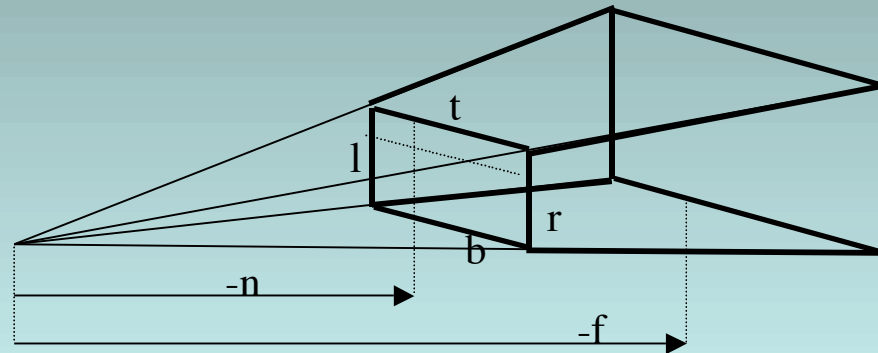
...



3D Projections

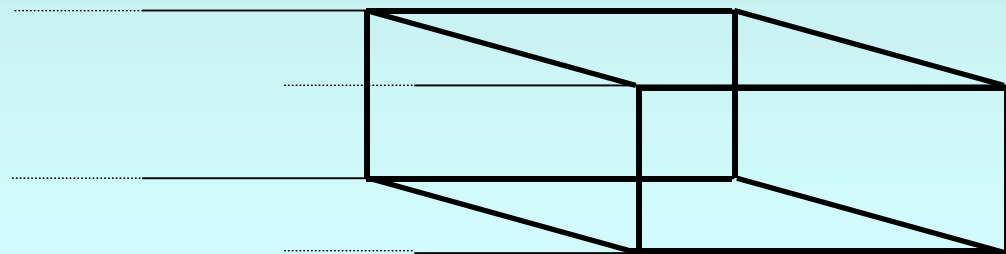
- Perspective Projection: `glFrustum* (l,r,b,t,n,f)`

$$\begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$



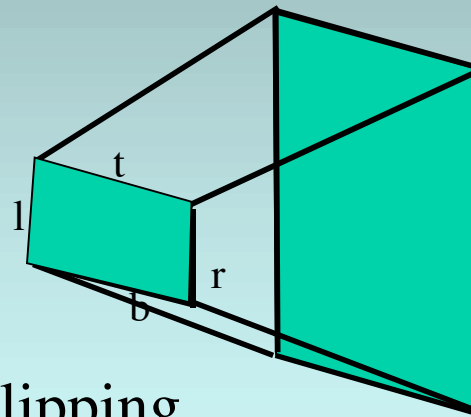
- Orthographic Projection: `glOrtho* (l,r,b,t,n,f)`

$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Viewport Transformation

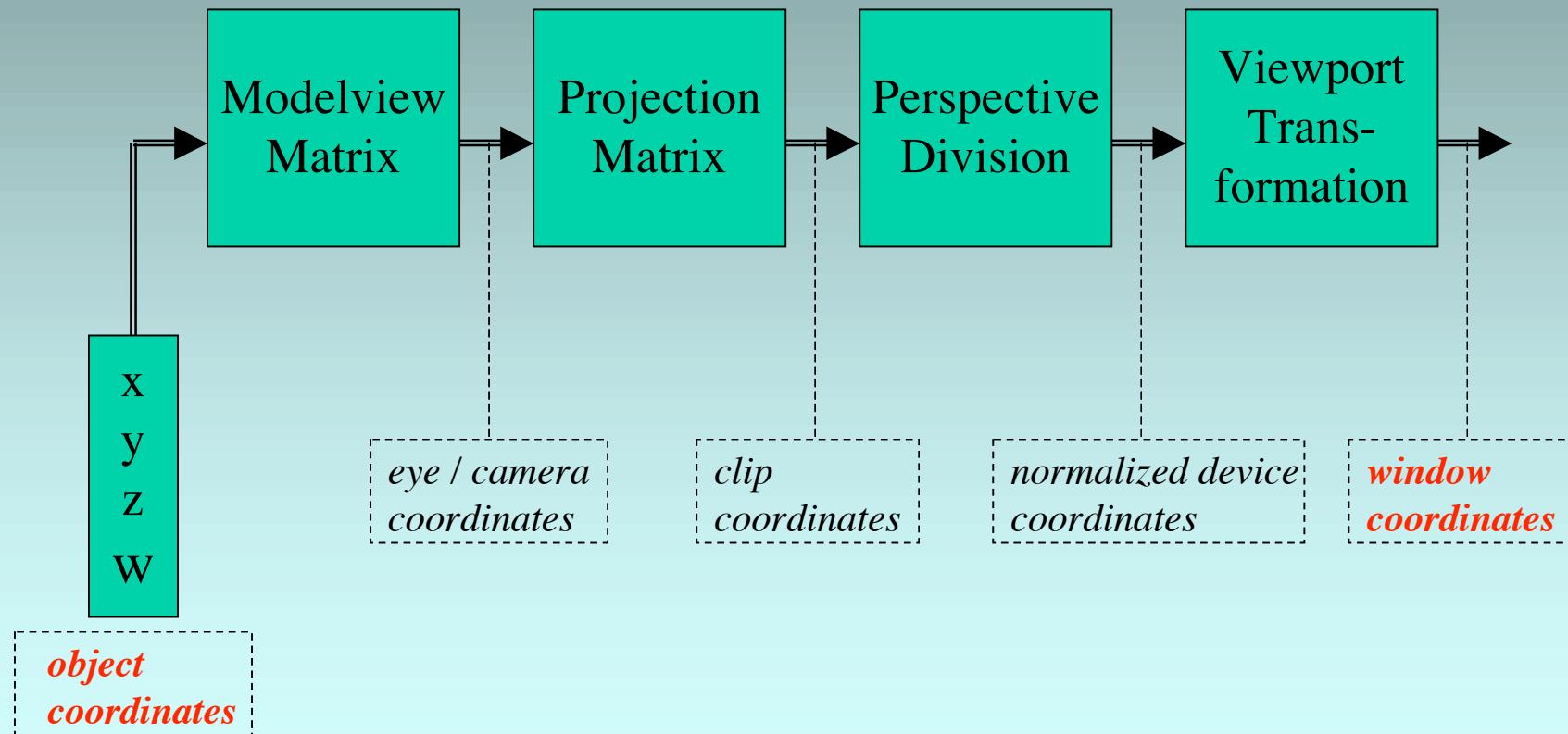
- `glViewport (x, y, width, height)`



window on
the screen

near clipping
plane of
frustum

Geometry Pipeline



Sample Code

```
// Viewport Transformations
```

```
glViewport (0.0, 0.0, w, h);
```

```
// Projection Transformations
```

```
glMatrixMode (GL_PROJECTION);
```

```
glLoadIdentity ();
```

```
glFrustum (l,r,t,b,n,f); or gluPerspective (60.0, w/h, 1.0, 20.0);
```

```
// Viewing Transformations
```

```
glMatrixMode (GL_MODELVIEW);
```

```
glLoadIdentity ();
```

```
glTranslatef (0.0, 0.0, -5.0); // move world away from camera
```

```
glRotatef (45.0, 0.0, 1.0, 0.0); // rotate world in front of the camera around y-axis
```

```
...
```

```
// Modeling Transformations
```

```
...
```

```
// Draw Object
```

