

# Einführung in die Erweiterte Realität

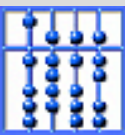
## 3. OpenGL, Mixing Virtual and Real Objects

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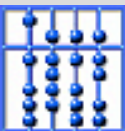
[klinker@in.tum.de](mailto:klinker@in.tum.de)

Nov 9, 2004



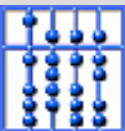
# Literature on the web

- <http://www.opengl.org/>
- <http://www.opengl.org/documentation/index.html>  
– redbook.pdf
- <http://www.opengl.org/resources/tutorials/>
- <http://www.opengl.org/resources/tutorials/overview.html>

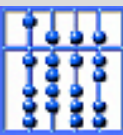


# Agenda

1. Event Loop and Window Management
2. Object Representations in OpenGL
3. Transformations
4. Graphical State Variables
5. Combinations of Virtual and Real Objects

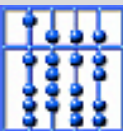


# 1. Event Loop and Window Management



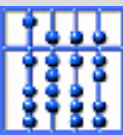
# Event Loop

```
Main () {  
  // ... some initializations:  
  // - open a window  
  // - initialize hardware on graphics card  
  // - initialize state variables (sw) in OGL driver  
  
  do { // EVENT LOOP  
    // ... loop initializations  
    // ... get events from windowing system (mouse, keyboard, etc)  
    // ... setup coordinate systems  
    // ... draw objects  
    // ... flush pipeline, swap buffers etc  
    // ... clean up  
  } while (TRUE); // infinite loop  
}
```



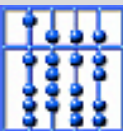
## GLUT: The OpenGL Utility Toolkit

- Communication with windowing systems to
  - Open, initialize, resize, ... windows
  - Receive input events from the windows
  - Draw into the windows
  - Routines to draw more complex objects



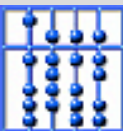
# Window management with GLUT

```
int main (int argc, char** argv) {  
    glutInit (&argc, argv);  
    glutInitDisplayMode (GLUT_SINGLE | GLUT_RGB);  
    glutInitWindowSize (250,250);  
    glutInitWindowPosition (100,100);  
    glutCreateWindow (“Hello”);  
    init(); // our own initializations  
    glutDisplayFunc(display);  
  
    glutMainLoop();  
    return 0;  
}  
  
void init (void) {}  
void display (void) {}
```



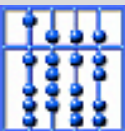
# Event management with GLUT

```
// event management  
void glutDisplayFunc (void (*func) (void))  
void glutReshapeFunc (void (*func)(int width, int height))  
void glutKeyboardFunc (void (*func)(unsigned int key, int x, int y))  
void glutMouseFunc (void (*func)(int button, int state, int x, int y))  
void glutMotionFunc (void (*func)(int x, int y))  
void glutPostRedisplay (void (*func)(void))  
  
// for animations  
void glutIdleFunc(void (*func) (void))  
  
// main loop (infinitely running)  
void glutMainLoop (void)
```





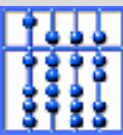
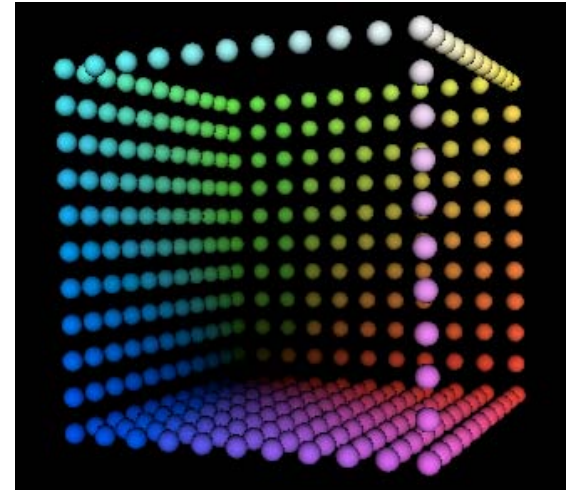
## 2. Object Representations in Open GL



# Object Representations in OpenGL

```
// draw a simple object  
// (a yellow square)  
glColor3f (1.0, 1.0, 0.0);
```

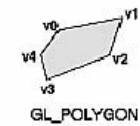
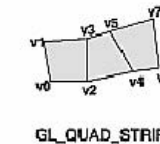
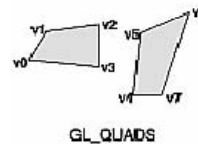
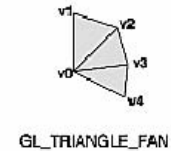
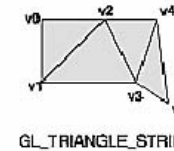
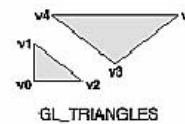
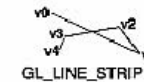
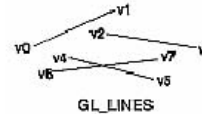
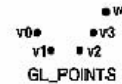
```
glBegin (GL_POLYGON);  
    glVertex3i (0, 0, 0);  
    glVertex3i (1, 0, 0);  
    glVertex3i (1, 1, 0);  
    glVertex3i (0, 1, 0);  
glEnd (...);
```



# glBegin (...)

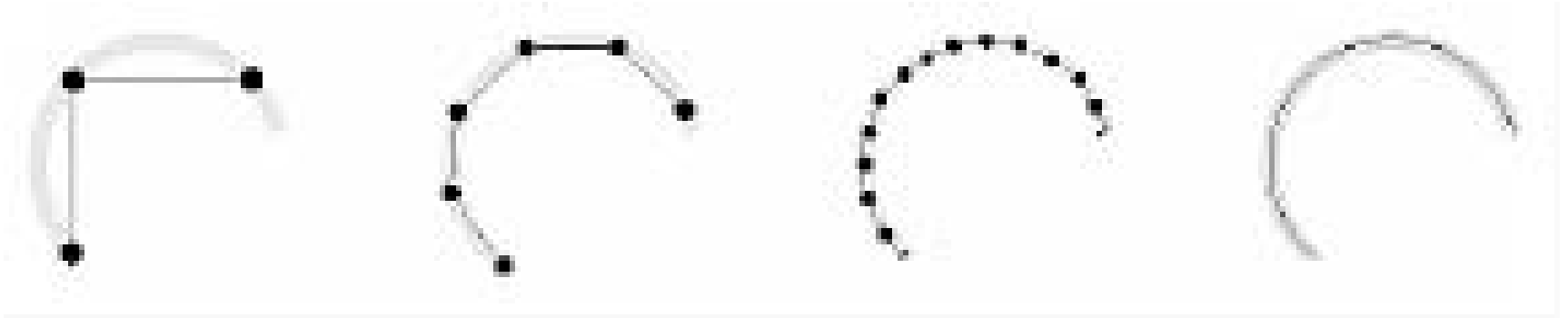
- **GL\_POINTS**
- **GL\_LINES**
- **GL\_LINE\_STRIP**
- **GL\_LINE\_LOOP**
- **GL\_TRIANGLES**
- **GL\_TRIANGLE\_STRIP**

- **GL\_TRIANGLE\_FAN**
- **GL\_QUADS**
- **GL\_QUAD\_STRIP**
- **GL\_POLYGON**



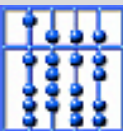
# More complex objects

- Approximation of a circle by a multi-edged polygon

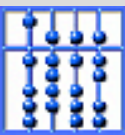


# More complex objects: Quadrics

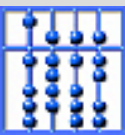
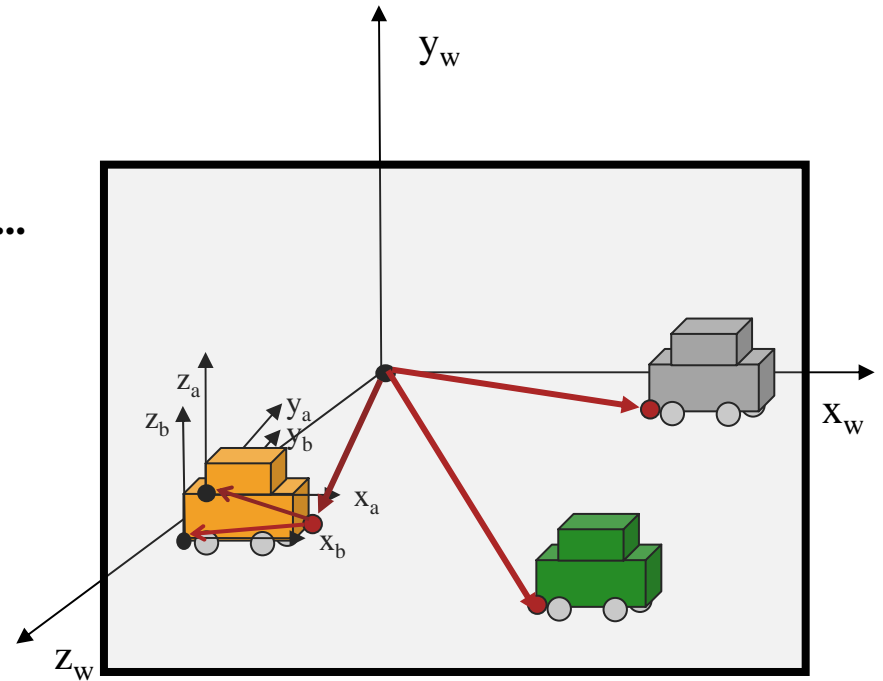
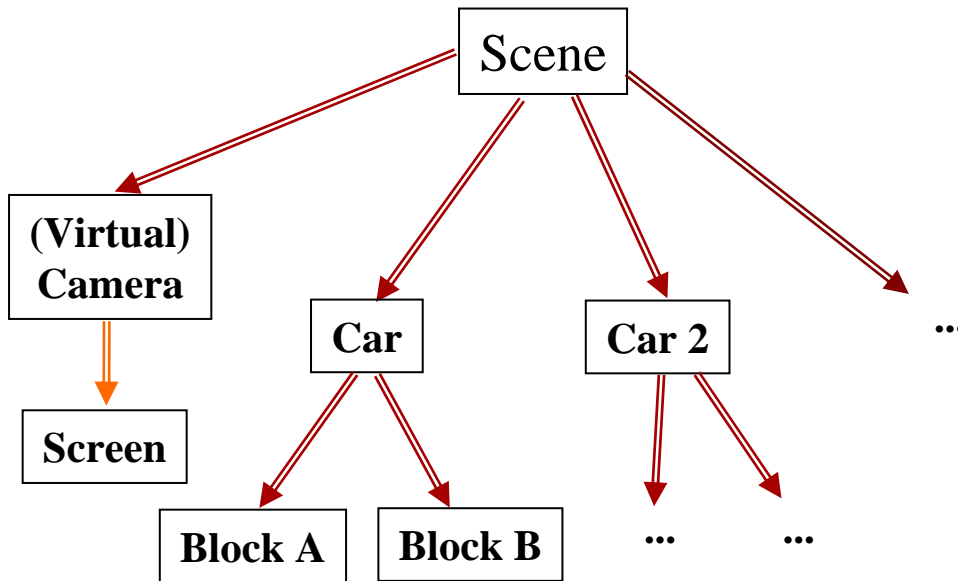
- **GLUQuadricObj \*obj = gluNewQuadric();**
  - ...
  - **gluSphere(obj,r,20,20);**
  - ...
  - **gluDeleteQuadric(obj);**
- **gluCylinder(...)**
  - **gluDisk(...)**
  - **gluPartialDisk(...)**
  - **gluSphere(...);**



# 3. Transformations



# Scene Graph



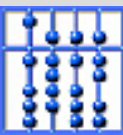
# 3D Transformations Using Homogeneous Coordinates

- Translation:  $\text{glTranslate}^*(t_x, t_y, t_z)$

$$\begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} x + wt_x \\ y + wt_y \\ z + wt_z \\ w \end{bmatrix}$$

- Scaling:  $\text{glScale}^*(s_x, s_y, s_z)$

$$\begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} s_x x \\ s_y y \\ s_z z \\ w \end{bmatrix}$$





# 3D Transformations Using Homogeneous Coordinates

- Rotation:  $\text{glRotate}^*(\alpha, \mathbf{e}_x, \mathbf{e}_y, \mathbf{e}_z)$

– around x

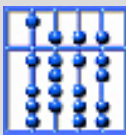
$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha & 0 \\ 0 & \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} x \\ \cos \alpha y - \sin \alpha z \\ \sin \alpha y + \cos \alpha z \\ w \end{bmatrix}$$

– around y

$$\begin{bmatrix} \cos \alpha & 0 & \sin \alpha & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \alpha & 0 & \cos \alpha & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} \cos \alpha x + \sin \alpha z \\ y \\ -\sin \alpha x + \cos \alpha z \\ w \end{bmatrix}$$

– around z

$$\begin{bmatrix} \cos \alpha & -\sin \alpha & 0 & 0 \\ \sin \alpha & \cos \alpha & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} \cos \alpha x - \sin \alpha y \\ \sin \alpha x + \cos \alpha y \\ z \\ w \end{bmatrix}$$

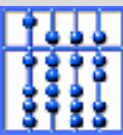


# Composition of Transformations

- Initialize accumulative matrix  $C_0$  with identity matrix  $I$
- Post-multiply accumulative matrix  $C_i$  with transformation matrix  $M_i$  according to command.  $C_{i+1} := C_i M_i$
- Accumulated result represents complete transformation (independent of the number of transformation steps)
- Transformation sequence not commutative!!!

Example: translate1 - scale1 - rotate1 - translate2 - rotate2

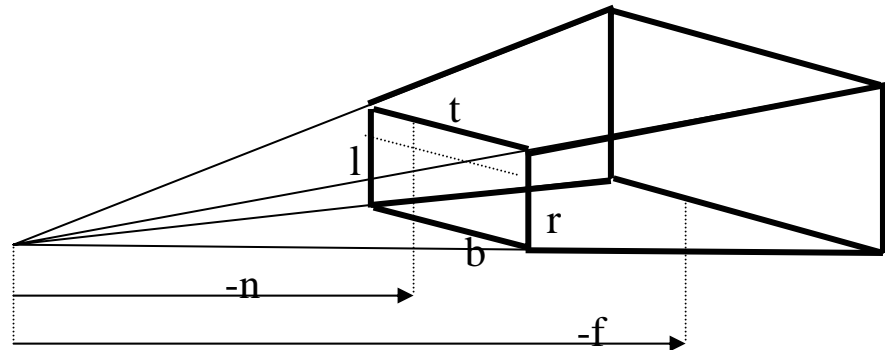
$$I * T1 * S1 * R1 * T2 * R2 * \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix}$$



# 3D Projections

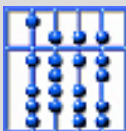
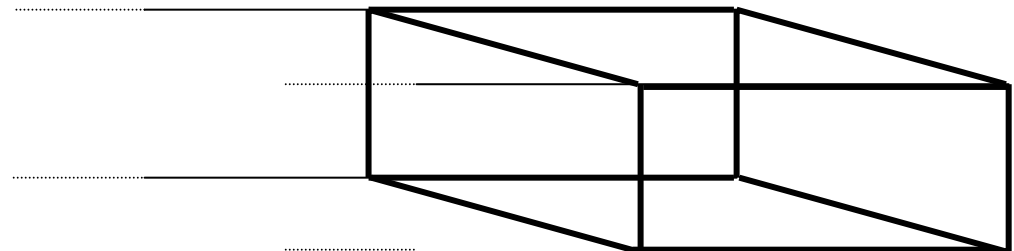
- Perspective Projection:  $\text{glFrustum}^*(l,r,b,t,n,f)$

$$\begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+1}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$



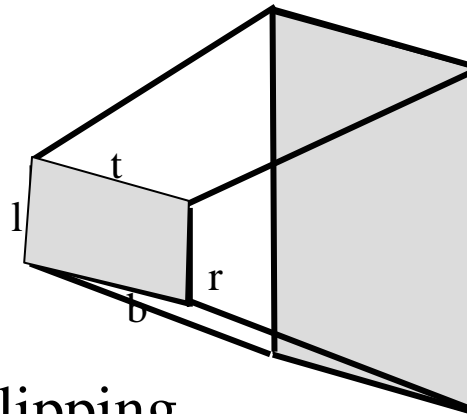
- Orthographic Projection:  $\text{glOrtho}^*(l,r,b,t,n,f)$

$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+1}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



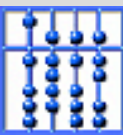
# Viewport Transformation

- `glViewport (x, y, width, height)`

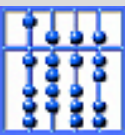
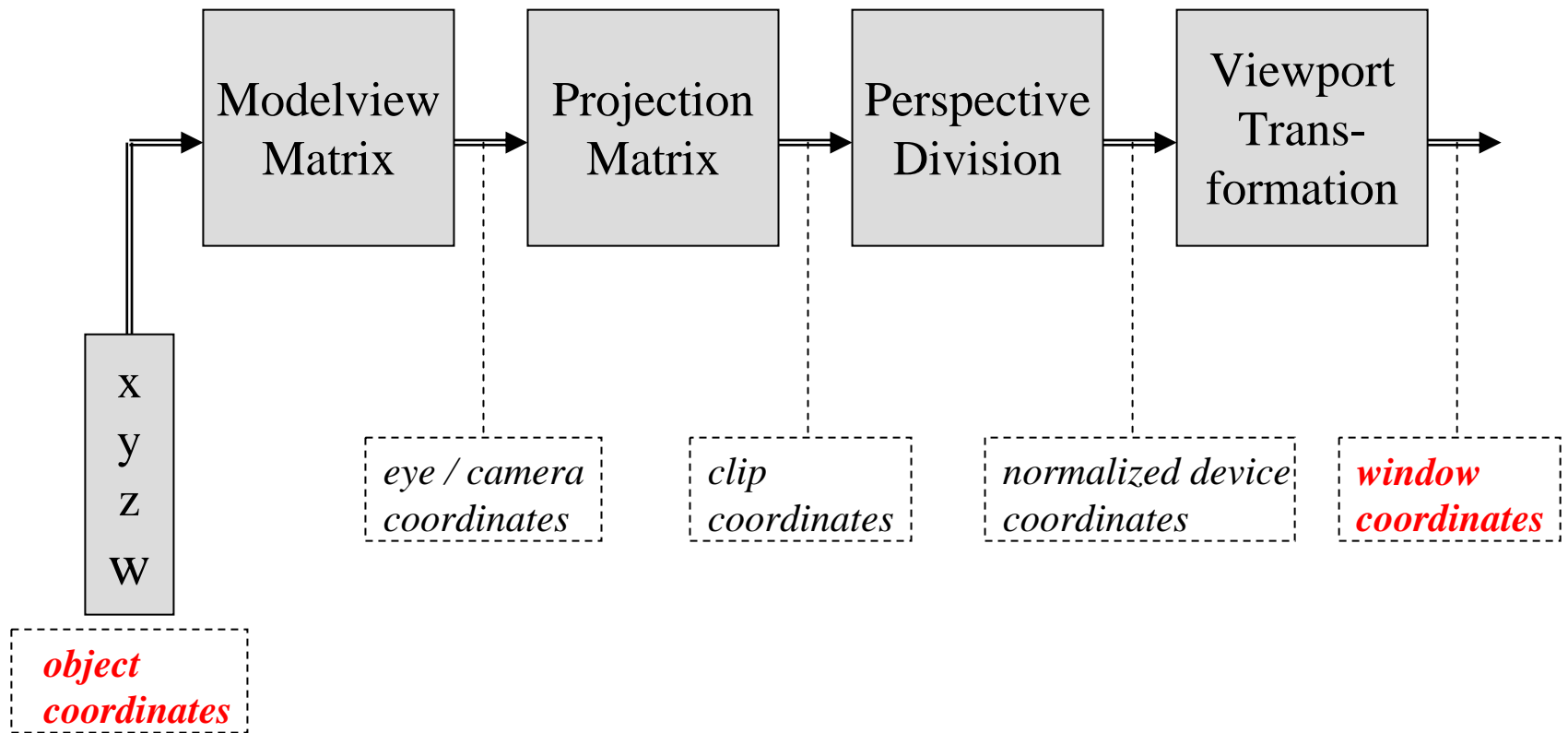


near clipping  
plane of  
frustum

window on  
the screen



# Geometry Pipeline

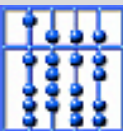
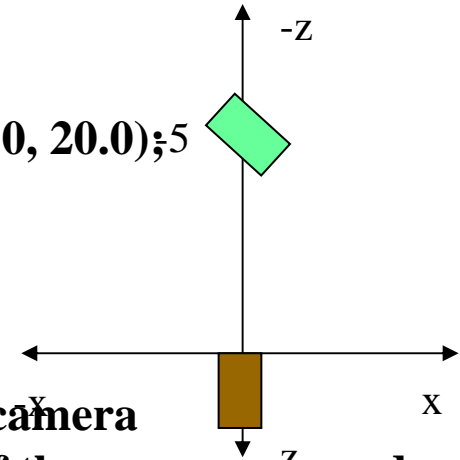


# Sample Code

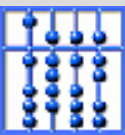
```
// Viewport Transformations
glViewport (0.0, 0.0, w, h);

// Projection Transformations
glMatrixMode (GL_PROJECTION);
glLoadIdentity ();
glFrustum (l,r,t,b,n,f);  or gluPerspective (60.0, w/h, 1.0, 20.0);5

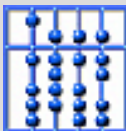
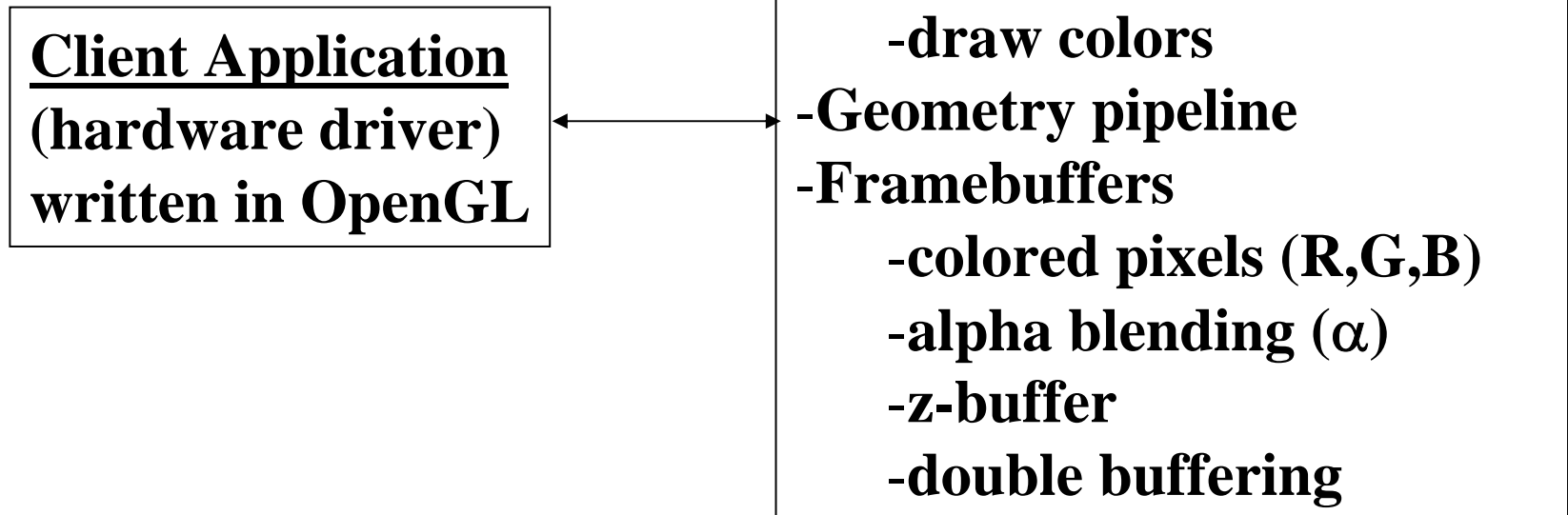
// Viewing Transformations
glMatrixMode (GL_MODELVIEW);
glLoadIdentity ();
glTranslatef (0.0, 0.0, -5.0); // move world away from camera
glRotatef (45.0, 0.0, 1.0, 0.0); // rotate world in front of the camera around y-axis
...
// Modeling Transformations
...
// Draw Object
...
```



# 4. Graphical State



# “Hardware-Driven View”





**glBegin(...)**

- **GL\_POINTS**
- **GL\_LINES**
- **GL\_LINE\_STRIP**
- **GL\_LINE\_LOOP**
- **GL\_TRIANGLES**
- **GL\_TRIANGLE\_STRIP**

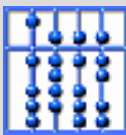
- **GL\_TRIANGLE\_FAN**

- **GL\_QUADS**

- **GL\_QUAD\_STRIP**

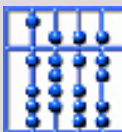
- **GL\_POLYGON**

**glEnd()**

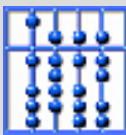


- for all:
  - Color (r,g,b): `glColor4f (1.0f,0.0f,0.0f,1.0f);`
- for Points:
  - Point size: `glPointSize(4.0f);`
- for Lines:
  - Line width: `glLineWidth (2.0f);`
  - Stipple patterns:  
`glEnable(GL_LINE_STIPPLE);`  
`glLineStipple (1,0xFFF0)`

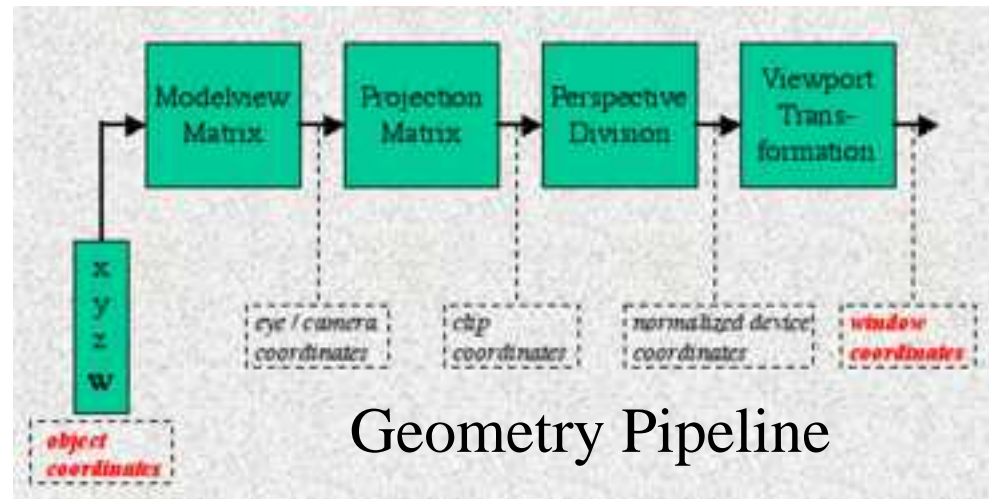
PATTERN	FACTOR	
0x00FF	1	_____
0x00FF	2	_____
0x0C0F	1	____ _
0x0C0F	3	_____
0xAAAA	1	- - - - -
0xAAAA	2	- - - - -
0xAAAA	3	____ _
0xAAAA	4	____ _



- for Polygons:
  - **glPolygonMode (GL\_BACK, GL\_LINE);**
    - **Points, outlines, solids:**  
{GL\_POINT, GL\_LINE, GL\_FILL}
    - **Front (counterclockw.) and/or back:**  
{GL\_FRONT, GL\_BACK, GL\_FRONT\_AND\_BACK}
  - **Culling: glCullFace (GL\_FRONT);**
    - {GL\_FRONT, GL\_BACK}
  - **Stippling patterns (32x32 bitmaps)**
  - **Normal vectors**

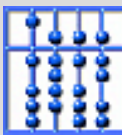
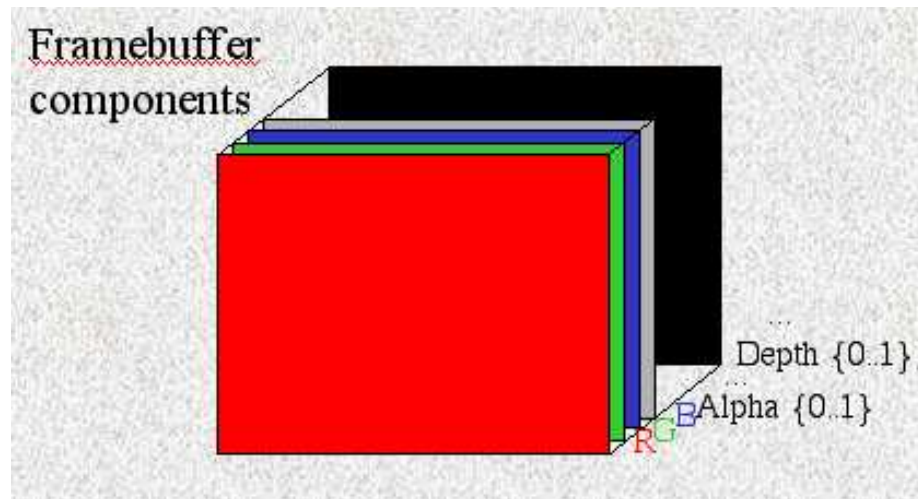


- **glMatrixMode (GL\_MODELVIEW);**
  - {GL\_MODELVIEW, GL\_PROJECTIONS}
- **glLoadIdentity();**
- **glTranslate (t<sub>x</sub>, t<sub>y</sub>, t<sub>z</sub>);**
- **glRotate (e<sub>x</sub>, e<sub>y</sub>, e<sub>z</sub>, angle);**
- **glScale (s<sub>x</sub>, s<sub>y</sub>, s<sub>z</sub>);**
- ...



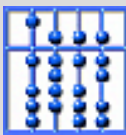
# State Variables: - Lighting, Textures, Framebuffer -

- **Lighting**
- **Texture Mapping**
- **Framebuffer Control**
  - **RGBA, depth, stencil, accumulation**
  - **Doublebuffering, stereo**



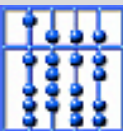
# Controlling the Grafical State

- Communication
  - **glFlush()**
- Functionality
  - **glEnable(...), glDisable(...)**
  - **glPushAttrib(...), glPopAttrib(...)**
  - **glPushMatrix(...), glPopMatrix(...)**
- Querying the graphical state
  - **glGetIntegerv(...)**
  - **glGetError(...)**
- Framebuffer control
  - **glClear(...), glClearColor(...), glClearDepth(...), ...**
  - **glXSwapBuffers()**

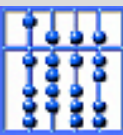


# Example

```
Main () {  
    // ... open a window in double buffer mode (depends on window system)...  
    glClearColor (0.0, 0.0, 0.0, 0.0); // black  
    glClearDepth (0.0);  
    glEnable (GL_DEPTH_TEST);  
    glDepthFunc (GL_LEQUAL);  
    do {  
        glClear (GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);  
        // ... coordinate transformations (viewing information)  
        glPushMatrix(); glPushAttrib(...);  
        // ... draw objects  
        glPopMatrix(); glPopAttrib(...);  
        // ... clean up  
        glFlush();  
        glXSwapBuffers (...);  
    } while (TRUE); // infinite loop  
}
```



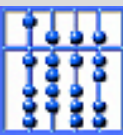
# 5. Combinations of Real and Virtual Objects





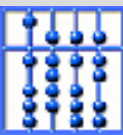
# Occlusions between Real and Virtual Objects

In Front In Back	Real Objects	Virtual Objects
Real Objects	optical occlusion	
Virtual Objects		

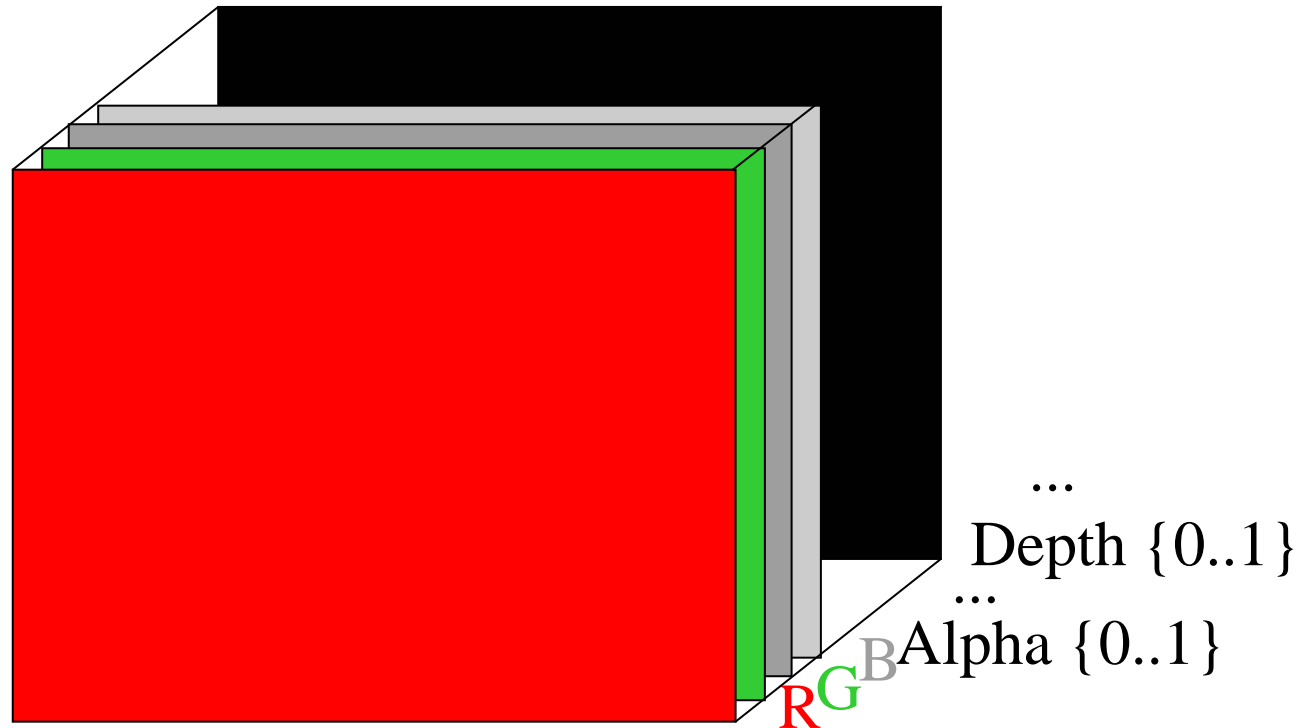


# Occlusions between Real and Virtual Objects

	In Front	Real Objects	Virtual Objects
In Back			
Real Objects		optical occlusion	
Virtual Objects			graphics hardware (z-buffering)

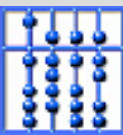


- Framebuffer components



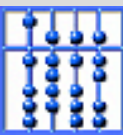
# Depth Buffer Manipulation

- **glClearDepth (1.0);**
- **glClear (GL\_DEPTH\_BUFFER\_BIT);**
- **glEnable (GL\_DEPTH\_TEST);**
- **glDepthFunc (GL\_LEQUAL);**
- **glDepthMask (GL\_TRUE);**



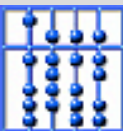
# Occlusions between Real and Virtual Objects

	In Front	Real Objects	Virtual Objects
In Back			
Real Objects		optical occlusion	graphics in front of video
Virtual Objects			graphics hardware (z-buffering)



# Drawing in the 2D image plane

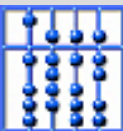
- **Orthographic view**  
`glOrtho (0,imgwidth, 0,imgheight, -1.0,1.0);`
- **Initialize modelling/viewing transformation**  
`glMatrixMode (GL_MODELVIEW);`  
`glLoadIdentity();`
- **Flip image (image array starts at upper left corner, OpenGL starts at lower left corner)**  
`glPixelZoom(1.0, -1.0);`
- **Define origin of image coordinate system:**  
`glRasterPos2i (0, imgheight);`

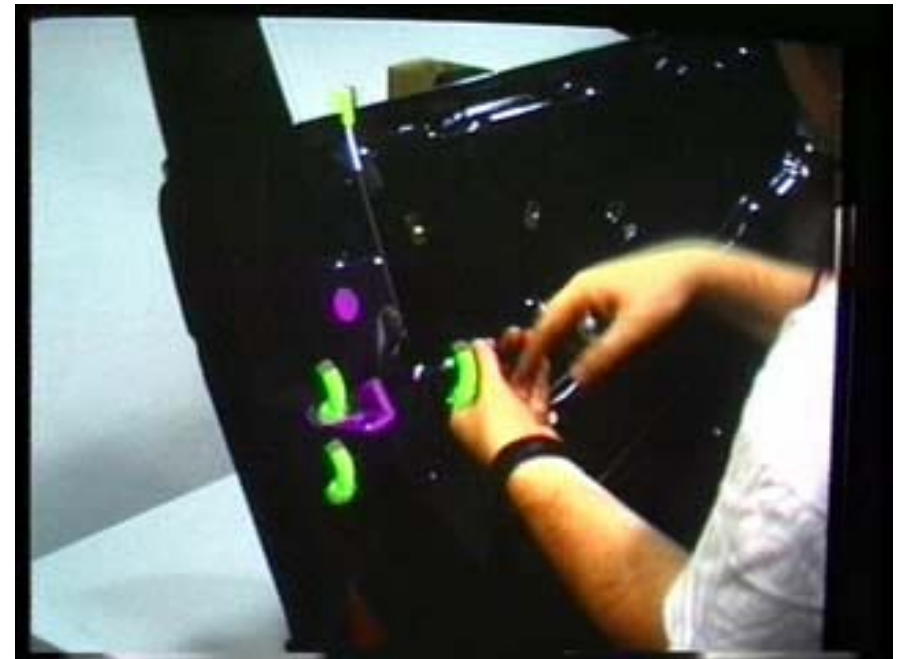
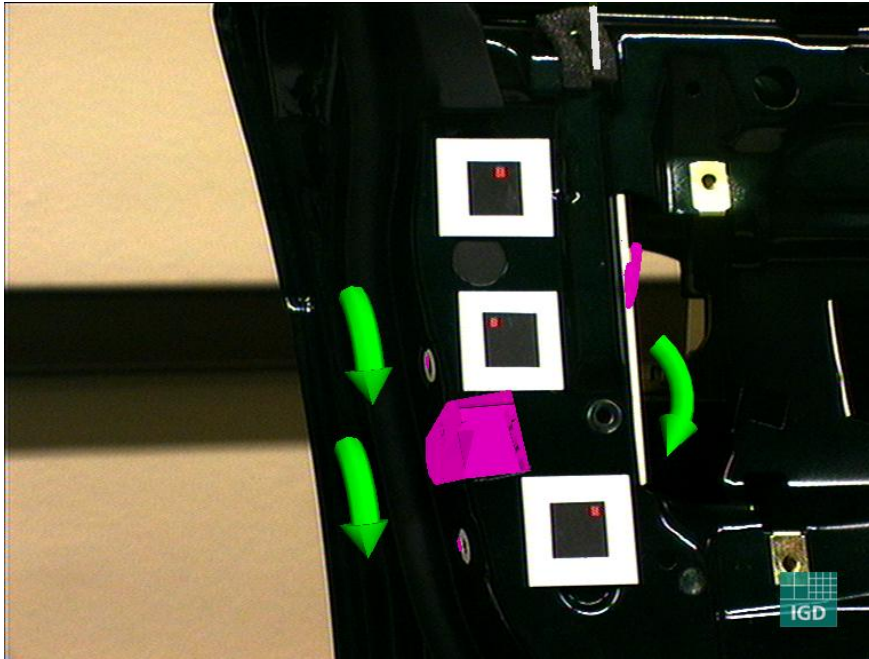


# Drawing 2D images and marks

- Draw image (upper left corner at raster pos)  
`glDrawPixels (imgwidth, imgheight, GL_RGBA,  
GL_UNSIGNED_BYTE, data);`
- Draw 2D marks (stored in a display-list) onto the image  
`glCallList (MyMarkers);`

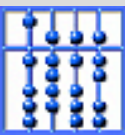
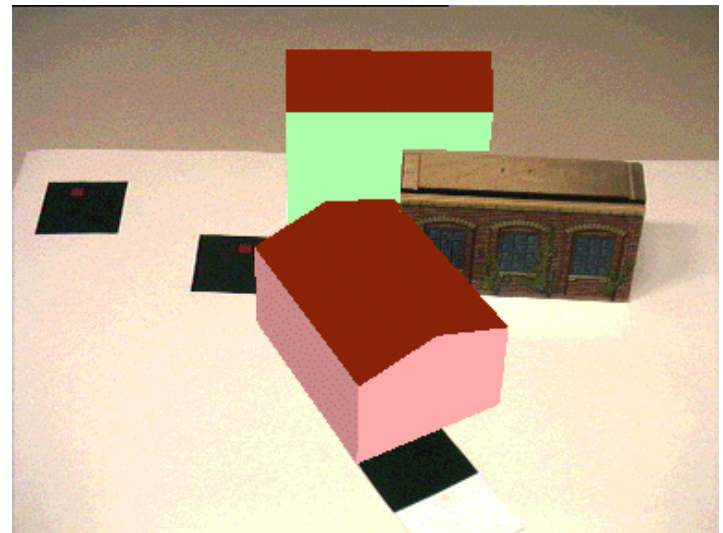
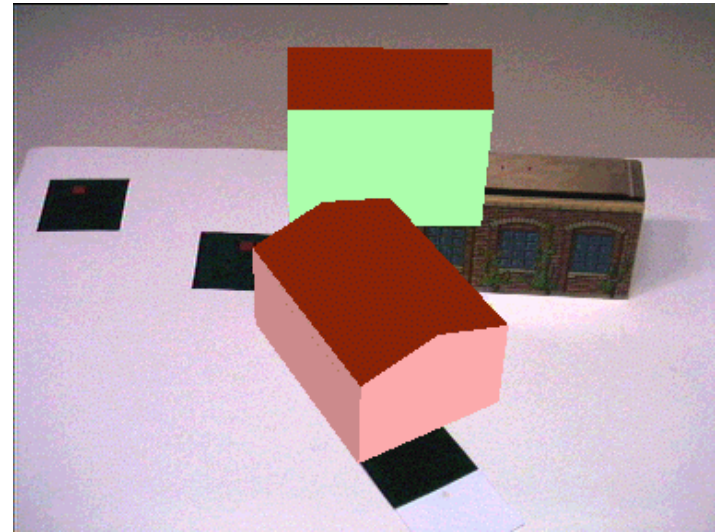
```
glNewList (MyMarkers, GL_COMPILE);  
    glBegin (GL_LINES);  
        glVertex2d (x, imgheight-y);  
        ....  
    glEnd ();  
glEndList ();
```





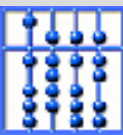


# Integrating Virtual Objects into a Real Scene



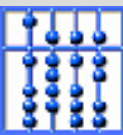
# Occlusions between Real and Virtual Objects

In Front	Real Objects	Virtual Objects
In Back		
Real Objects	optical occlusion	graphics in front of video
Virtual Objects	<b>video + transparent reality models + opaque virtual models</b>	graphics hardware (z-buffering)

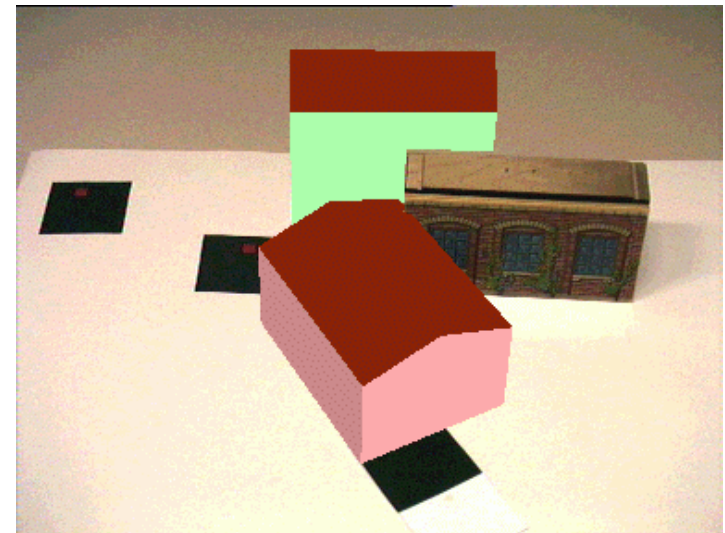
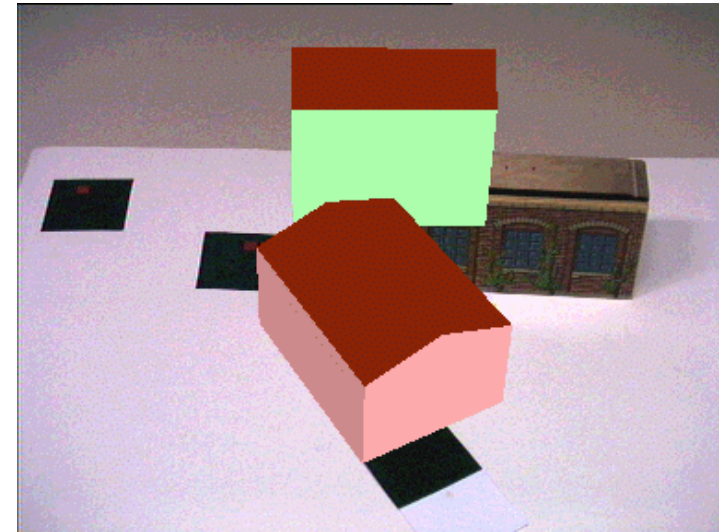
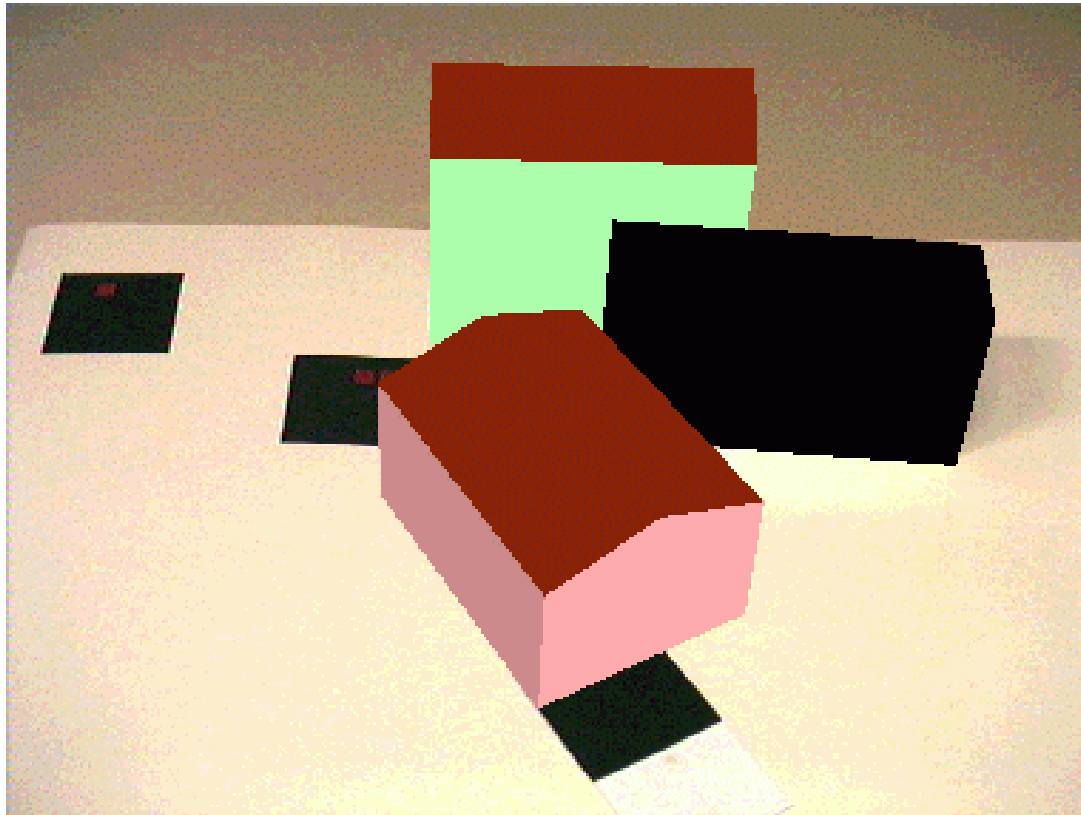


# Integrating Virtual Objects into a Real Scene

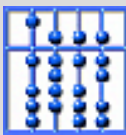
- Prerequisites:
  - Obtain geometrically precise models of all real objects.
  - Determine the current position of mobile objects.
- For a given camera position:
  - Draw video image (as background).
  - Initialize depth buffer.
  - Draw transparent models of real objects.
  - Draw opaque models of virtual objects.

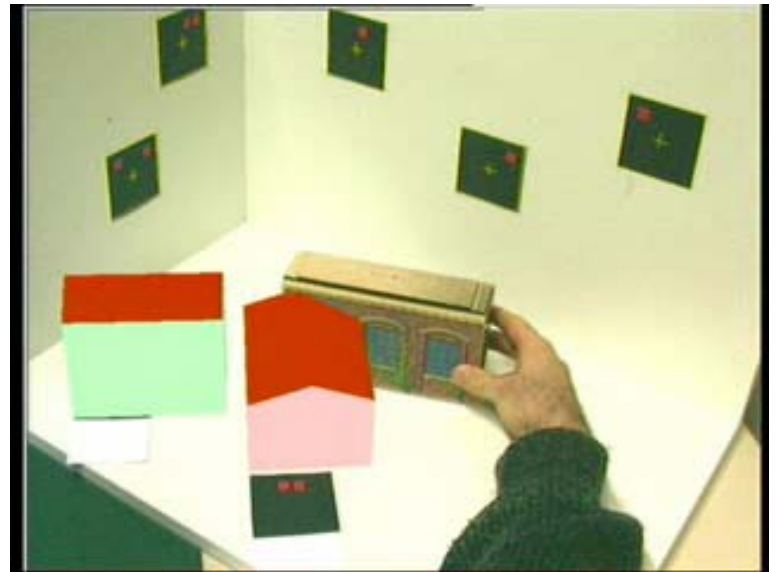
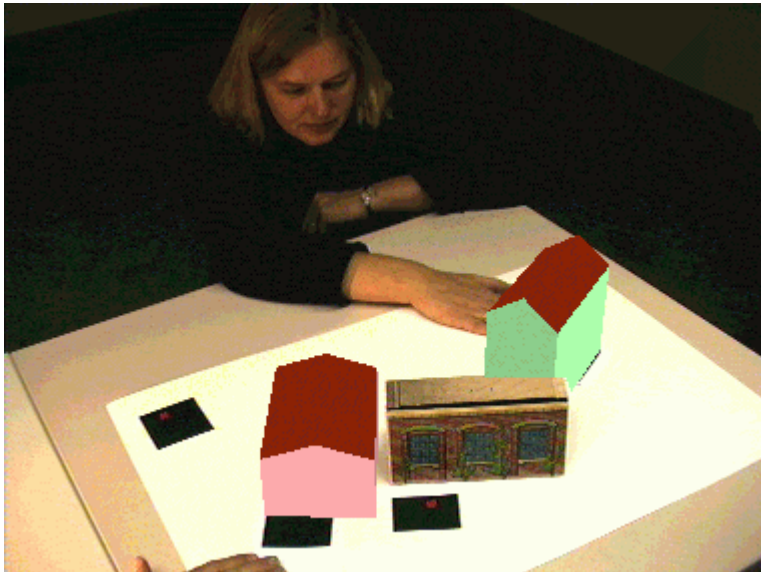


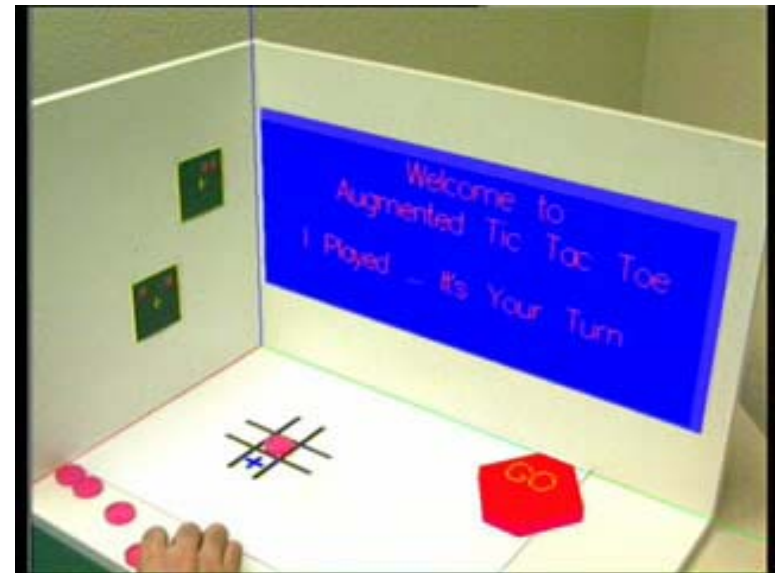
# Integrating Virtual Objects into a Real Scene



- ...Draw video image
- ...Initialize depth buffer
- `glColorMask (GL_FALSE, GL_FALSE, GL_FALSE, GL_FALSE);`
- ...Draw reality model
- `glColorMask (GL_TRUE, GL_TRUE, GL_TRUE, GL_TRUE);`
- ...Draw virtual model







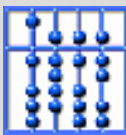


# Transparency via Pixel Blending

Updated pixel color  $[x,y] =$   
 $S * \text{new color } [x,y]$  “source”  
 $+ D * \text{current color } [x,y]$  “destination”

$$\begin{pmatrix} R \\ G \\ B \\ A \end{pmatrix} = \begin{pmatrix} R_s & S_r \\ G_s & S_g \\ B_s & S_b \\ A_s & S_a \end{pmatrix} + \begin{pmatrix} R_d & D_r \\ G_d & D_g \\ B_d & D_b \\ A_d & D_a \end{pmatrix}$$

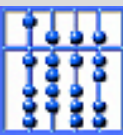
$\uparrow$  *Source factor*                       $\uparrow$  *Destination factor*





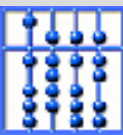
# Blending Factors

- **GL\_ZERO (0, 0, 0, 0)**
- **GL\_ONE (1, 1, 1, 1)**
- **GL\_DST\_COLOR** ( $R_d, G_d, B_d, A_d$ )
- **GL\_SRC\_COLOR** ( $R_s, G_s, B_s, A_s$ )
- **GL\_ONE\_MINUS\_DST\_COLOR** ( $1-R_d, 1-G_d, 1-B_d, 1-A_d$ )
- **GL\_ONE\_MINUS\_SRC\_COLOR** ( $1-R_s, 1-G_s, 1-B_s, 1-A_s$ )
- **GL\_SRC\_ALPHA** ( $A_s, A_s, A_s, A_s$ )
- **GL\_ONE\_MINUS\_SRC\_ALPHA** ( $1-A_s, 1-A_s, 1-A_s, 1-A_s$ )
- **GL\_DST\_ALPHA** ( $A_d, A_d, A_d, A_d$ )
- **GL\_ONE\_MINUS\_DST\_ALPHA** ( $1-A_d, 1-A_d, 1-A_d, 1-A_d$ )
- **GL\_SRC\_ALPHA\_SATURATE** ( $f, f, f, 1$ )  $f=\min(A_s, 1-A_d)$



# Examples of blending combinations

- **GL\_SRC\_ALPHA, GL\_SRC\_ALPHA**;  $\alpha = 0.5$
- **GL\_SRC\_ALPHA, GL\_ONE\_MINUS\_SRC\_ALPHA**;  $\alpha = 0.25$
- **GL\_SRC\_ALPHA, GL\_ONE**;  $\alpha = 1/n$  (for  $n$  images)
- **GL\_ZERO, GL\_ONE** (for transparent models of real objects)



- **...Draw video image**
- **...Initialize depth buffer**
- **glEnable (GL\_BLEND);**
- **glBlendFunc (sfactor=0, dfactor=1);**
- **...Draw reality model**
- **glBlendFunc (sfactor=1, dfactor=0);**
- **...Draw virtual model**

